

**ERRATA AND ADDITIONS FOR  
DYNAMICAL SYSTEMS: STABILITY, SYMBOLIC DYNAMICS, AND CHAOS**

BY CLARK ROBINSON

(\*) Corrected in second printing.

Also see the list of Corrections for the Second Edition of the book.

- p. 20: (L. 8) “ $x \in I$ ” should be “ $x \in I \setminus \{p\}$ ”
- p. 22: (L. 5-8) This should read as follows: A direct calculation shows that for  $2 < \mu < 3$  the only fixed points of  $F_\mu^2$  are those for  $F_\mu$ , i.e., 0 and  $p_\mu$ . (See Exercise 2.6.) Since  $F_\mu^2(1/2)$  is above the diagonal, it follows that  $F_\mu^2(x)$  is above the diagonal and  $x < F_\mu^2(x) < p_\mu$  for  $1/2 \leq x < p_\mu$ . Therefore all the points in the interval  $[1/2, p_\mu]$  converge to  $p_\mu$  under iteration by  $F_\mu^2$ . Since  $|F'_\mu(p_\mu)| < 1$ , it follows that all these points converge to  $p_\mu$  under iteration by  $F_\mu$  as well.
- p. 22: (L. 7) “below  $1/2$ ” should be “below  $p_\mu$ ”
- p. 23: (L. -18) “implies” should be “imply”
- p. 24: (L. 2) “ $d(f^n(x), \omega(x))$ ” should be “ $d(f^n(x), \alpha(x))$ ”
- p. 24: (L. 7) This should read as follows: Similarly, if  $f$  is invertible and  $\mathbf{y} \in \alpha(\mathbf{x})$  then  $\alpha(\mathbf{y}) \subset \alpha(\mathbf{x})$  and  $\omega(\mathbf{y}) \subset \alpha(\mathbf{x})$ .
- p. 24: (L. -9) “invariant” should be “positively invariant”
- p. 24: (L. -3) “ $S$  is closed” should be “ $S$  is a closed”
- p. 25: (L. 12) This should read as follows: . . . , although there are other . . .
- p. 28: (L. -9) remove “expansions have nonunique representations.”
- p. 32: (L. -4) “ $\leq \lambda|b - a|$ ” should be “ $\geq \lambda|b - a|$ ”
- p. 34: (L. 10) . . . derivative of  $f$  is always nonzero on the interval  $J$ , . . .
- p. 39: (L. 4) A stronger condition is . . .
- p. 39: (L. -9) . . . we describe such a point for  $p = 2$ . (An obvious change gives the general case.)  
Let  $\mathbf{t}$  be a . . .
- p. 39: (L. -3) Therefore  $d(\sigma^n(\mathbf{t}), \mathbf{s}) \leq 3^{1-k}2^{-1}$ .
- p. 40 (L. 10) In the last section we showed
- p. 40 (L. -7) “onto” is not needed since it is part of the definition of semi-conjugacy.
- p. 42: (L. -8) change “ $2|z|$ .” to “ $2|z|$ ,”
- p. 44: (L. 11) “ $h \circ f(x) = g \circ h$ ” should be “ $h \circ f(x) = g \circ h(x)$ ”
- p. 44: (L. -19) “and and” should be “and”
- p. 44: (L. -7)

$$= \lim_{\substack{x \rightarrow 1 \\ x > 1}} h'_0(x).$$

Typeset by  $\mathcal{A}\mathcal{M}\mathcal{S}\text{-}\mathcal{T}\mathcal{E}\mathcal{X}$

- p. 44: (L. -4) Now let  $\{x_i\}$  be an arbitrary sequence with  $x_i \neq 0$  that ...
- p. 44: (L. -1) “ $h_0$ ” should be “ $h$ ”
- p. 47: (L. 11) “ $[-2, 0] \cup [1, 2]$ .” should be “ $[-2, 0] \cup [1, 2]$ ,”
- p. 51: (L. -6) “ $p \geq F^n(0) < p + 1$ ” should be “ $p \leq F^n(0) < p + 1$ ”
- p. 55: (L. 7) “ $F_7^{n_2^2}(0) + m_1$ ” should be “ $F_7^{n_2^2}(0) + m_2$ ”
- \*p. 57: (2.6c) Prove for any point  $x$  with  $0 < x < 1$  that either (i) there is an integer  $k \geq 0$  such that  $F_\mu^k(x) = p_\mu$  where  $p_\mu$  is the fixed point or (ii) the  $\omega(x)$  is the orbit of period 2.
- p. 58: (2.7d) ... Then prove that  $W^s(\mathcal{O}(q)) = (-p, 0) \cup (0, p) \setminus \mathcal{O}^-(0)$  where  $\pm p$  are two of the fixed points and  $\mathcal{O}^-(0)$  is the backward orbit of the origin.
- p. 58: (2.8c) “ $\mathcal{O}^+(\mathbf{p}) = \omega(\mathbf{p})$ ” should be “ $\mathcal{O}^+(\mathbf{p}) \supset \omega(\mathbf{p})$ ”
- p. 58: (2.11) “ $F'_\mu(x) > 2$ ” should be “ $|F'_\mu(x)| > 2$ ”
- p. 58: (2.12) “ $|f'_\mu(x)|\rho(f_\mu(x))/\rho(x)$ ” should be “ $|F'_\mu(x)|\rho(F_\mu(x))/\rho(x)$ ”
- p. 59: (2.16a) “ $I_{s_0 \dots s_n 0}$  to the left of  $I_{s_0 \dots s_n 1}$ ” should be “ $I_{s_0 \dots s_n 1}$  to the left of  $I_{s_0 \dots s_n 2}$ ”
- p. 60: (2.18) “ $|x_j - f^j(x)| < \epsilon$ ” should be “ $|x_j - F_\mu^j(x)| < \epsilon$ ”
- p. 60: (2.16b) Remove the sentence “What effect does having a symbol 2 (where the slope is negative on  $I_2$ ) have on the order of the intervals?”
- p. 61: (2.25) ... that are topologically conjugate by an orientation preserving homeomorphism.  
...
- p. 61: “ $0 \leq i < n$ ” should be “ $0 \leq i < p$ ”
- p. 80: (L. 3) “slight” should be “slightly”
- p. 80: (L. 3) “slight” should be “slightly”
- p. 90: (3.13) It should read “Let  $\Lambda = \bigcap_{n=0}^{\infty} f^{-n}(I)$ .”
- p. 101 (3.8d) I  $M(t)$  is a mtrix solution of the constant coefficient equation (\*\*) with  $M(0)$  non-singular, then
- p. 132: (L. -7 to -4) Replace with: “If  $U$  is a region where  $f(\mathbf{x})$  is defined and  $C^1$  and  $V \subset U$  is a compact subset, then we can let  $K = \sup\{\|Df_{\mathbf{x}}\| : \mathbf{x} \in V\}$ . By the Mean Value Theorem,

$$|f(\mathbf{x}) - f(\mathbf{y})| \leq K|\mathbf{x} - \mathbf{y}|$$

if the line segment from  $\mathbf{x}$  to  $\mathbf{y}$  is contained in  $V$ .

- p. 133: (L. 26–27) These lines should read as follows:

$$\begin{aligned} B(\mathbf{v}, \mathbf{w}) &= \sum_{\ell=1}^n \left( \sum_{1 \leq i, j \leq k} b_{i,j}^\ell v_i w_j \right) \mathbf{s}^\ell \\ &= \sum_{1 \leq i, j \leq k} \left( \sum_{\ell=1}^n b_{i,j}^\ell \mathbf{s}^\ell \right) v_i w_j. \end{aligned}$$

- p. 141 (Line 7–9) For  $\mathbf{x}_0 \in U$  take  $b > 0$  such that the closed ball  $\bar{B}(\mathbf{x}_0, b) \equiv \{\mathbf{x} : |\mathbf{x} - \mathbf{x}_0| \leq b\} \subset U$ . The function  $f$  is Lipschitz ... for all  $\mathbf{x}, \mathbf{y} \in \bar{B}(\mathbf{x}_0, b)$ .
- p. 179: (Theorem 9.1) The region does not have to be simply connected. It should read: “either an open subset of  $\mathbb{R}^2$  or  $\mathcal{D} = S^2$ .”
- \*p. 193: (L. 8) “ $(\lambda - \epsilon\alpha^{-1})^n 2r$ ” should be “ $(\lambda - \epsilon\alpha^{-1})^{-n} 2r$ ”

- p. 195: (L. 6) See the separate sheet for an extended addition.
- p. 208: (5.40) It should read: “Assume that  $\tilde{X}_1(x, a) < 0$ ,  $\tilde{X}_1(x, b) > 0$ , and  $\tilde{X}_2(x, a) = 0 = \tilde{X}_2(x, b)$  for all  $x$ ,”
- p. 215: (L. 4) “th” should be “the”
- p. 215: (L. 9) “directions” should be “subspace”
- p. 215: (L. 10) “include” should be “includes”
- p. 217: (L. -9) It should be “ $+2\left(\frac{\partial^2 f_1}{\partial x_1 \partial x_j}(\mathbf{x}_0, \mu_0)\right)\left(\frac{\partial \phi}{\partial x_1}(a, \mu_0)\right)$ ”
- \*p. 230: (L. -2) “ $F_\mu(0, 0)\left(\frac{-F_{\epsilon\epsilon}(0, 0)}{F_\mu(0, 0)}\right)\epsilon^2$ ” should be “ $F_\mu(0, 0)\left(\frac{-F_{\epsilon\epsilon}(0, 0)}{2F_\mu(0, 0)}\right)\epsilon^2$ ”
- \*p. 232: (6.6) (a) ... for  $4A = 3(1 + B_0)^2$ . (b) ... at  $A = 3(1 + B_0)^2/4$  as  $A$  varies ...
- p. 233: (6.10) The differential equation should read

$$\dot{z} = -\frac{8}{3} + xy$$

- \*p. 236: (L. 16) ... is called an *immersion* provided the derivative of  $\phi$  at each point is an isomorphism. The image of a one to one immersion is called an *immersed submanifold*. If an immersion is a homeomorphism then it is called an *embedding* and its image is called an *embedded submanifold*. (Some people require that an embedding is also proper, i.e., the inverse image of a compact set is compact.)
- \*p. 241: (L. 13) “ $T_{\mathbf{p}}$ ” should be “ $T_{\mathbf{p}}M$ ”
- p. 241: (L. 15) (iv) there exist  $0 < \lambda < 1$  and  $C \geq 1$  independent of  $\mathbf{p}$  such that for all  $n \geq 0$  and for all  $\mathbf{p} \in \Lambda$ ,
- \*p. 242: (L. 1) First sentence should be: Assume  $\Lambda$  is a hyperbolic invariant set for  $f$  with constants  $0 < \lambda < 1$  and  $C \geq 1$  giving the hyperbolic structure.
- p. 243: (L. -7, -9) These two line should read

$$= \bigcup_{n \geq 0} f^{-n}(W_\epsilon^s(f^n(\mathbf{p}), f))$$

and

$$= \bigcup_{n \geq 0} f^n(W_\epsilon^u(f^{-n}(\mathbf{p}), f)).$$

- p. 248 (Line 8-10) In both the definitions of adjacency matrix and transition matrix add the conditions that (ii)  $\sum_j a_{ij} \geq 1$  for all  $i$ , and (iii)  $\sum_i a_{ij} \geq 1$  for all  $j$ .
- p. 256: (L. 10) It takes some argument that  $\bigcap_{j=-n}^n F^j(S)$  has  $4^n$  components. Any curve  $\gamma$  in  $S$  from  $x = -3$  to  $x = 0$  has an image  $F(\gamma)$  which reaches in  $S$  from  $x = -3$  to  $x = 3$ . Similarly, any curve  $\gamma$  in  $S$  from  $x = 0$  to  $x = 3$  has an image  $F(\gamma)$  which reaches in  $S$  from  $x = -3$  to  $x = 3$ . Applying this to the the top and bottom boundaries of the strips in  $F(S) \cap S$  shows that  $\bigcap_{j=0}^2 F^j(S)$  has four strips all the way across  $S$  from  $x = -3$  to  $x = 3$ . (There could be other components with just this argument. After proving the existence of invariant cones, it follows there are exactly four components.) By induction,  $\bigcap_{j=0}^n F^j(S)$  has  $2^n$  “horizontal” strips which reach all the way across  $S$  from  $x = -3$  to  $x = 3$ . A similar argument applies to  $F^{-1}$  to show that  $\bigcap_{j=-n}^0 F^j(S)$  is made up of  $2^n$  “vertical” strips which reach all the way across  $S$  from  $y = -3$  to  $y = 3$ . A horizontal strip must intersect a vertical

strip in at least one component. Therefore  $\bigcap_{j=-n}^n F^j(S)$  has at least  $4^n$  components. These are nested as  $n$  increases.

- p. 256: (L. -11,-10) In the definition of the cones, “ $T_{\mathbf{p}}M$ ” should be “ $T_{\mathbf{p}}\mathbb{R}^2$ ” on both lines.
- p. 258: (L. -6) Compare with the argument on the separate extended addition to page 195.
- p. 259: (L. -1) A horseshoe is any isolated invariant set which is (i) hyperbolic, (ii) zero topological dimension, and (iii) topologically transitive. By using the existence of a Markov partition, Theorem IX.6.1, a diffeomorphism restricted to such an invariant set is conjugate to a subshift of finite type.
- \*p. 260: (L. 11) itinerary
- p. 262: (L. 4-10) For simplicity below, we take an adapted metric on  $\Lambda_{\mathbf{q}}$ . (The adapted metric implies that for  $\mathbf{x} \in \Lambda_{\mathbf{q}}$ ,  $Df_{\mathbf{x}}$  is an immediate contraction on  $\mathbb{E}_{\mathbf{x}}^s$  and an immediate expansion on  $\mathbb{E}_{\mathbf{x}}^u$ .) We extend the splitting  $\mathbb{E}_{\mathbf{x}}^s \oplus \mathbb{E}_{\mathbf{x}}^u$  on  $\Lambda$  to a continuous (probably noninvariant) splitting  $\hat{\mathbb{E}}_{\mathbf{x}}^s \oplus \hat{\mathbb{E}}_{\mathbf{x}}^u$  on a (perhaps smaller) neighborhood  $V$  of  $\Lambda_{\mathbf{q}}$ . We use cones to show there is an invariant splitting which approximates  $\hat{\mathbb{E}}_{\mathbf{x}}^s \oplus \hat{\mathbb{E}}_{\mathbf{x}}^u$  and extends the splitting  $\mathbb{E}_{\mathbf{x}}^s \oplus \mathbb{E}_{\mathbf{x}}^u$  on  $\Lambda_{\mathbf{q}}$ . For  $\mathbf{x} \in V$ , using the adapted metric let

$$C^s(\mathbf{x}) = \{(\xi, \eta) \in \hat{\mathbb{E}}_{\mathbf{x}}^s \oplus \hat{\mathbb{E}}_{\mathbf{x}}^u : |\eta| \leq \mu|\xi|\}$$

and

$$C^u(\mathbf{x}) = \{(\xi, \eta) \in \hat{\mathbb{E}}_{\mathbf{x}}^s \oplus \hat{\mathbb{E}}_{\mathbf{x}}^u : |\xi| \leq \mu|\eta|\}$$

some  $0 < \mu < 1$ .

- \*p. 271: (L. 20) ... so we want to measure  $\hat{G}(\mathbf{z}_0, \epsilon) = H(\mathbf{z}^u(\mathbf{z}_0, \epsilon)) - H(\mathbf{z}^s(\mathbf{z}_0, \epsilon))$ . Since  $\hat{G}(\mathbf{z}_0, 0) \equiv 0$ , it is possible to write  $\hat{G}(\mathbf{z}_0, \epsilon) = \epsilon G(\mathbf{z}_0, \epsilon)$ . A zero of ...
- p. 298: (Step 2) Compare with the argument on the separate extended addition to page 195.
- p. 271: (L. 3b) **Proof** (of Theorem 4.6) We want to apply the Implicit Function Theorem to the function  $G$ . We know that  $G(\mathbf{z}_0, 0) = M(\mathbf{z}_0) = 0$  and

$$\frac{\partial G}{\partial \mathbf{v}}(\mathbf{z}_0, 0) = \frac{\partial M}{\partial \mathbf{v}}(\mathbf{z}_0) \neq 0.$$

Let  $\Sigma$  be a transversal to the flow at  $\mathbf{z}_0$  which contains the direction  $\mathbf{v}$ . Applying the Implicit Function Theorem to  $G$  restricted to  $\Sigma$ , there is a function  $\mathbf{z}^*(\epsilon)$  such that  $G(\mathbf{z}^*(\epsilon), \epsilon) \equiv 0$ , i.e.,  $\mathbf{z}^*(\epsilon)$  is a homoclinic point for small enough  $\epsilon$ . The fact that the homoclinic point is transversal follows from the fact that the derivative is not zero.

- p. 291 (L. 15) It should read

$$= \prod_{k=0}^n \det(I - tf_{*k})^{(-1)^{k+1}},$$

without the superscript  $j$  on  $f_{*k}$ .

- \*p. 321: (L 11-12) “ $\hat{W}^s(\mathcal{O}(\mathbf{p}_j)) \cap \hat{W}^s(\mathcal{O}(\mathbf{p}_{j+1})) \neq \emptyset$ ” should be “ $\hat{W}^u(\mathcal{O}(\mathbf{p}_j)) \cap \hat{W}^s(\mathcal{O}(\mathbf{p}_{j+1})) \neq \emptyset$ ”
- \*p. 323: (Thm 12.3) “ $\frac{\partial^2 V}{\partial x_i \partial x_j}(\mathbf{x})$ ” should be “ $\left(\frac{\partial^2 V}{\partial x_i \partial x_j}(\mathbf{x})\right)$ ”
- p. 327 (7.13) Assume  $A$  is irreducible.
- \*p. 328: (7.19) This refers to Example 4.1 on page 267, and not the one of page 253.
- \*p. 328: (7.22) Let  $f_A$  be a hyperbolic toral automorphism on  $\mathbb{T}^n$  with lift  $L_A$  to  $\mathbb{R}^n$ . Let  $g$  be a small  $C^1$  perturbation of  $f_A$  with lift  $G$  to  $\mathbb{R}^n$ . Finally, let  $\hat{G} = G - L_A$ . Let  $C_{b,per}^0(\mathbb{R}^n)$ ,  $C_{b,per}^1(\mathbb{R}^n)$ , and  $\Theta(\hat{G}, v)$  be defined as in the proof of Theorem 5.1.

- (a) Prove that  $\hat{G} \in C_{b,per}^1(\mathbb{R}^n)$ .  
 (b) Prove that  $\Theta(\hat{G}, \cdot)$  preserves  $C_{b,per}^0(\mathbb{R}^n)$ .  
 p. 329: (Improved wording for 7.25) (A horseshoe as a subsystems of a hyperbolic toral automorphism.) Let  $f_{A_2} : \mathbb{T}^2 \rightarrow \mathbb{T}^2$  be the diffeomorphism induced by the matrix

$$A_2 = \begin{pmatrix} 2 & 1 \\ 1 & 1 \end{pmatrix}$$

discussed in Example 5.4. Let  $R_{1a}$  be the rectangle used in the Markov partition for this diffeomorphism. Let  $g = f_{A_2}^2$  and

$$\Lambda = \bigcap_{j=-\infty}^{\infty} g^j(R_{1a}).$$

Prove that  $g : \Lambda \rightarrow \Lambda$  is topologically conjugate to the two-sided full two-shift  $\sigma : \Sigma_2 \rightarrow \Sigma_2$ . Hint:  $R_{1a}$  plays the role that  $S$  played in the construction of the geometric horseshoe. Prove that  $g(R_{1a}) \cap R_{1a}$  is made up of two disjoint rectangles. (These rectangles are similar to  $V_1$  and  $V_2$  in the geometric horseshoe.) Looking at the transition matrix for the Markov partition for  $f_{A_2}$  may help.

- p. 335: (Thm 1.2) The only thing that needs to be changed in the proof of Theorem 1.2 is to say “taking the limits in  $n$  and then  $\eta$ ”. Note that  $\epsilon \leq \eta$ , so as  $\eta$  goes to zero,  $\epsilon$  also must do to zero.  
 p. 344 (L. -9) This should read: “By letting  $\epsilon$  go to zero,  $h_{sep}(K, f) = h_{span}(K, f)$ .”  
 p. 360 (Example 4.1:) The map should be

$$f(t, z) = (g(t), \beta z + \frac{1}{2}e^{2\pi ti})$$

- p. 364 (Ex. 8.28) It should read  $f(t, z) = (g(t), \beta z + \frac{1}{2}e^{2\pi ti})$ .  
 (a) Prove for  $0 < \beta < 1/(2\sqrt{2})$ , ...  
 p. 368: (Theorem 1.1) ... has a Liapunov function  $L$  such that (i)  $L$  is strictly decreasing off  $\mathcal{R}(\phi^t)$ , (ii) if  $L(\mathbf{x}) = L(\mathbf{y})$  for  $\mathbf{x}, \mathbf{y} \in \mathcal{R}(\phi^t)$  then  $\mathbf{x} \sim \mathbf{y}$ , and (iii)  $L(\mathcal{R}(\phi^t))$  is nowhere dense.  
 \*p. 369: (L. 8) “Proposition 1.10” should be “Proposition 1.9”  
 \*p. 369: (L. 18-22) (b) The proofs that attracting sets and repelling sets are invariant are similar, so we only look at  $A$ . Let  $\mathbf{x} \in A$  and fix any real  $s$ . Then  $\mathbf{x} \in \phi^t(U)$  for all  $t \geq 0$ , so  $\phi^s(\mathbf{x}) \in \phi^{t+s}(U)$ . Therefore,  $\phi^s(\mathbf{x}) \in \bigcap_{t \geq |s|} \phi^{t+s}(U) = A$ . Since  $s$  is arbitrary,  $A$  is both positively and negatively invariant.  
 \*p. 370: (L. 6) Since  $\mathbf{y} \notin U$ ,  $\mathbf{y} \notin A$ . From the definition of  $\Omega_\epsilon^+$ , it follows that there is a  $T > 0$  such that  $\phi^T(\mathbf{y}) \in U$  so  $\phi^T(\mathbf{y}) \notin A^*$ . But Proposition 1.2 proves that ...  
 \*p. 370: (L. -8) Therefore, if  $\mathbf{x} \notin A^*$ , then  $V(\phi^t(\mathbf{x}))$  goes to zero  
 p. 372: (Theorem 1.8) ... a Liapunov function  $L : M \rightarrow \mathbb{R}$  such that (i)  $L$  is strictly decreasing off  $\mathcal{P}$ , (ii) if  $L(\mathbf{x}) = L(\mathbf{y})$  for  $\mathbf{x}, \mathbf{y} \in \mathcal{P}$  then  $\mathbf{x} \sim \mathbf{y}$ , and (iii)  $L(\mathcal{P})$  is nowhere dense.  
 p. 372: (L. 24) If  $\mathbf{x}, \mathbf{y} \in \mathcal{P}$  and  $\mathbf{x} \not\sim \mathbf{y}$  then there is a  $k$  such that one of the points is in  $A_k$  and the other is in  $A_k^*$ , so  $L_k(\mathbf{x}) \neq L_k(\mathbf{y})$  and  $L(\mathbf{x}) \neq L(\mathbf{y})$ .  
 p. 380: (L. -4) “ $\leq \delta + \epsilon$ ” should be “ $\leq \nu + \epsilon$ ”.  
 p. 385: (L. 8) there is a  $\mathbf{p}' \in H_{\mathbf{p}}$  and  $\mathbf{q}' \in H_{\mathbf{q}}$  such that ...

- p. 398: (Theorem 7.1) This should read: ...  $f : M \rightarrow M$  is an Anosov diffeomorphism ( $f$  has a hyperbolic structure on all of  $M$ ).
- p. 400: (L. -5) ... and so is a conjugacy.
- p. 402: (L. 3) is an stable disk at  $\mathbf{x}$
- p. 402: (L. 6-9) By construction of the disks and definition of  $F^t$ ,

$$(\phi^t(\mathbf{x}), \psi^{\tau(t, \mathbf{x}, h(\mathbf{x}))}(h(\mathbf{x}))) = F^t(\mathbf{x}, h(\mathbf{x})) \in D^u(\phi^t(\mathbf{x}), \eta) \cap D^s(\phi^t(\mathbf{x}), \eta),$$

but also

$$(\phi^t(\mathbf{x}), h \circ \phi^t(\mathbf{x})) \in D^u(\phi^t(\mathbf{x}), \eta) \cap D^s(\phi^t(\mathbf{x}), \eta),$$

so by uniqueness of this point

$$h \circ \phi^t(\mathbf{x}) = \psi^{\tau(t, \mathbf{x}, h(\mathbf{x}))}(h(\mathbf{x})).$$

- p. 402: (Proposition 8.2) A flow  $\phi^t$  is called *flow expansive* on  $\Lambda$  provided given  $\epsilon > 0$ , there exists a  $\delta > 0$  such that if  $\mathbf{x}_1, \mathbf{x}_2 \in \Lambda$  with

$$d(\phi^t(\mathbf{x}_1), \phi^{\sigma(t)}(\mathbf{x}_2)) < \delta$$

for all  $t$  where

$$\lim_{t \rightarrow \pm\infty} \sigma(t) = \pm\infty,$$

then  $\mathbf{x}_2 = \phi^s(\mathbf{x}_1)$  for some  $|s| \leq \epsilon$ .

- p. 407: (L. 5) Exercise 9.38 should be Exercise 9.37.
- p. 408: (L. 5)

$$“d(D^{-i}(x_j), x_{j-i}) \leq \delta \left( \frac{1}{q} + \dots + \frac{1}{q^i} \right) \leq \delta”$$

should be

$$“d(D^{-i}(x_j), x_{j-i}) \leq \delta \left( \frac{1}{2} + \dots + \frac{1}{2^i} \right) \leq \delta.”$$

- p. 409: (Problem 22) It is necessary to assume that all points are nonwandering. (Problem 22b) Prove that  $W^s(\mathbf{q})$  is dense in  $M$ .
- p. 427: (L. 2-3) These should be “ $-\hat{f}(\mathbf{x})D(\beta_r)_\mathbf{x}$ ” not “ $+\hat{f}(\mathbf{x})D(\beta_r)_\mathbf{x}$ ”
- p. 427: (L. -3) ... the transversality condition with respect to  $\mathcal{R}(f)$ .
- p. 428 (L. 3-5) Assume  $f$  is  $C^1$  structurally stable. Then by Theorem 4.3 (or Exercise 10.11(c)), it then follows that  $f$  also satisfies the transversality condition with respect to  $\mathcal{R}(f)$ .
- p. 434: (L. -7) ... complete spaces (closed balls in normed linear spaces) since ...
- p. 438: (L. -3)

$$\angle(C^u) = \sup \left\{ \frac{|\mathbf{w} - \mathbf{w}'|}{|\mathbf{v}|} : (\mathbf{v}, \mathbf{w}), (\mathbf{v}, \mathbf{w}') \in C^u \subset T_\mathbf{x}X \times Y \right\}.$$

- p. 439: (L. -9) Compare with the argument on the separate extended addition to page 195.
- p. 443: (L. 18) “Since the invariant section has  $\mathbb{E}_\mathbf{x}^u$  as a graph, the unstable bundle is  $C^1$ .” should be “By uniqueness, the invariant section has  $\mathbb{E}_\mathbf{x}^u$  as a graph and the unstable bundle is  $C^1$ .”

The following people were some of those who told me about errata in the book: Youngna Choi, James Jacklitch, Ming-Chia Li, Jody Sorensen, and Dick Swanson.

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