Homework 4

- 1. a. Prove that the Cantor set C consists of precisely those numbers in [0, 1] that can be written as $\sum_{k=1}^{\infty} \frac{a_k}{3^k}$ with all $a_k \in \{0, 2\}$.
 - **b**. Prove using the definition of the Cantor-Lebesgue function given in class that it is constant on every interval contained in $[0, 1] \sim C$.
- 2. Royden, Section 2.7, Exercise 41.
- **3**. Royden, Section 2.7, Exercise 44.
- 4. Royden, Section 2.7, Exercise 46.
- 5. Royden, Section 2.7, Exercise 47.